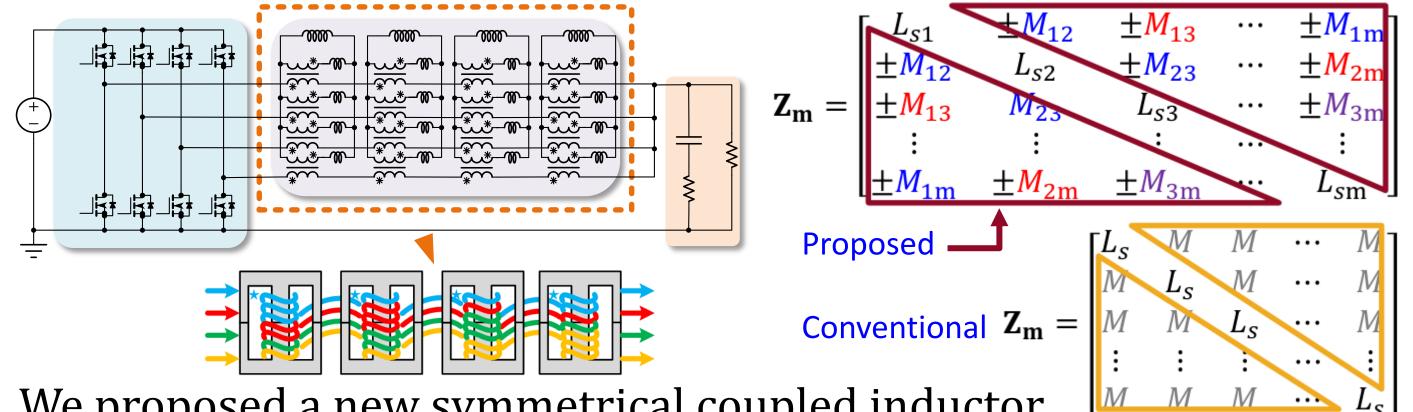


## Discrete Symmetrical Coupled Inductor Structure and its Matrix-type Implementation for DC-DC Converter

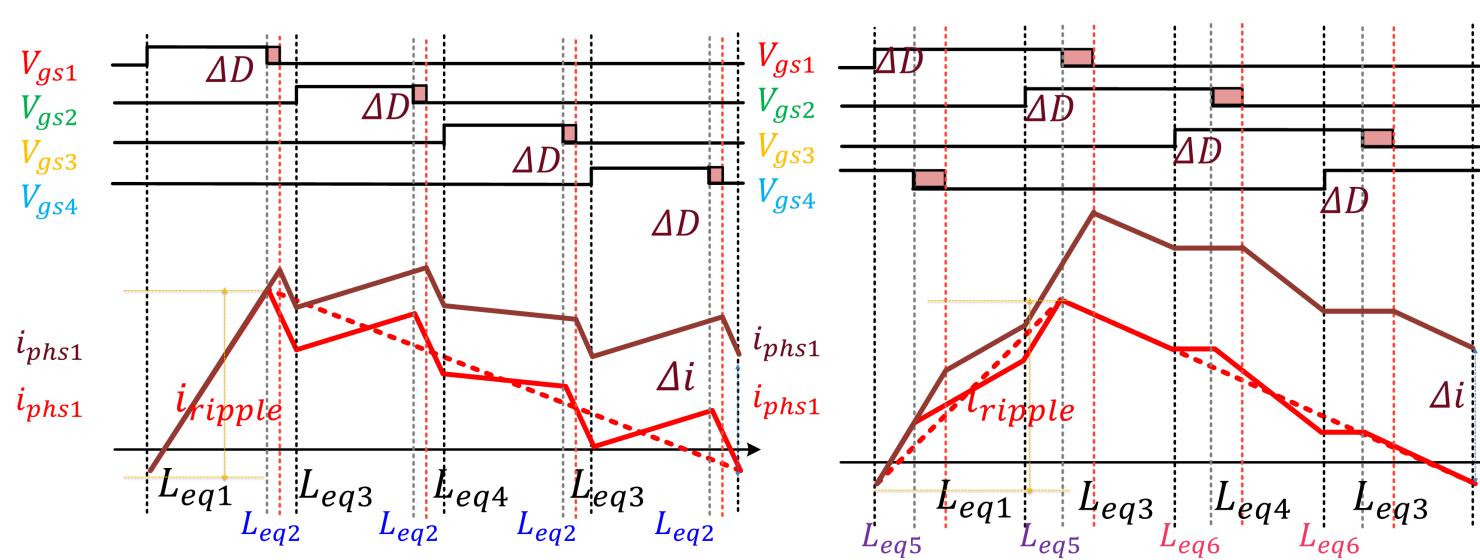
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We proposed a new symmetrical coupled inductor
structure for dc-dc converters, the main difference is the mutual inductance between phases can be either positive or negative

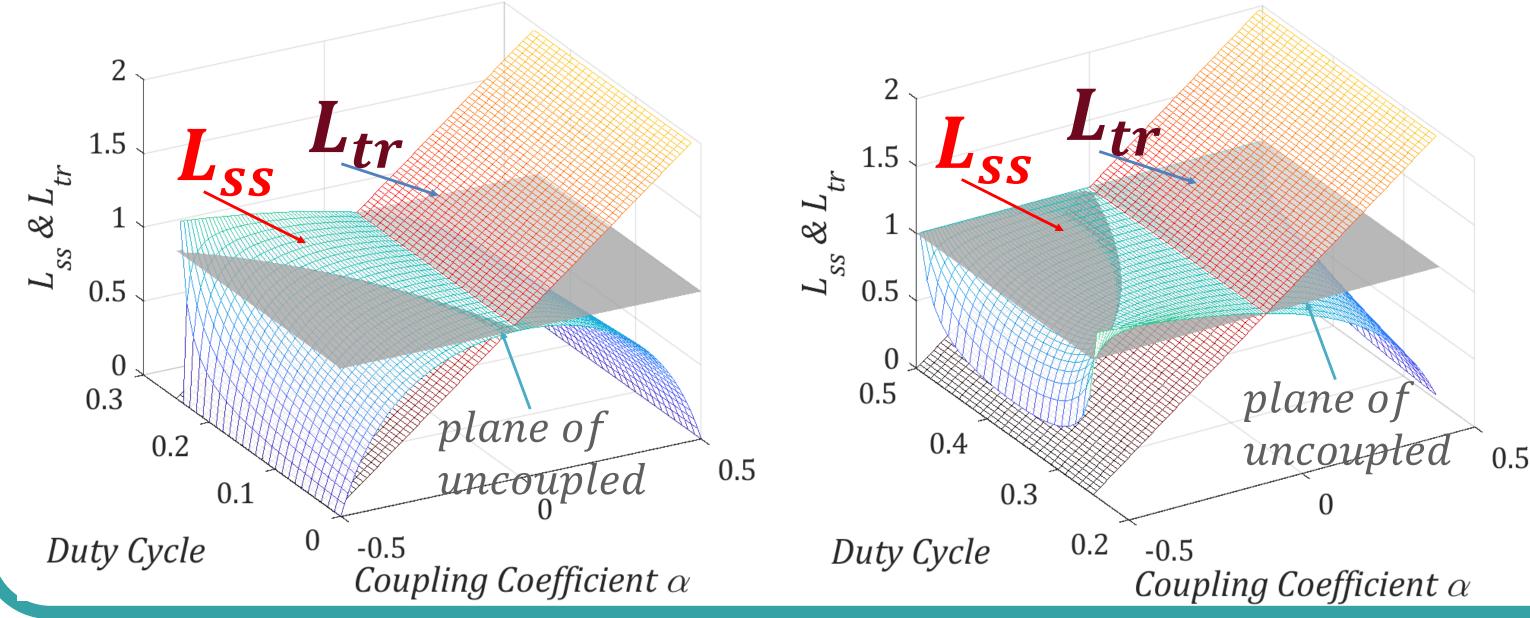


Phase current can analyzed under time intervals, with its equivalent interval inductance, related to the duty cycle and coupling coefficient

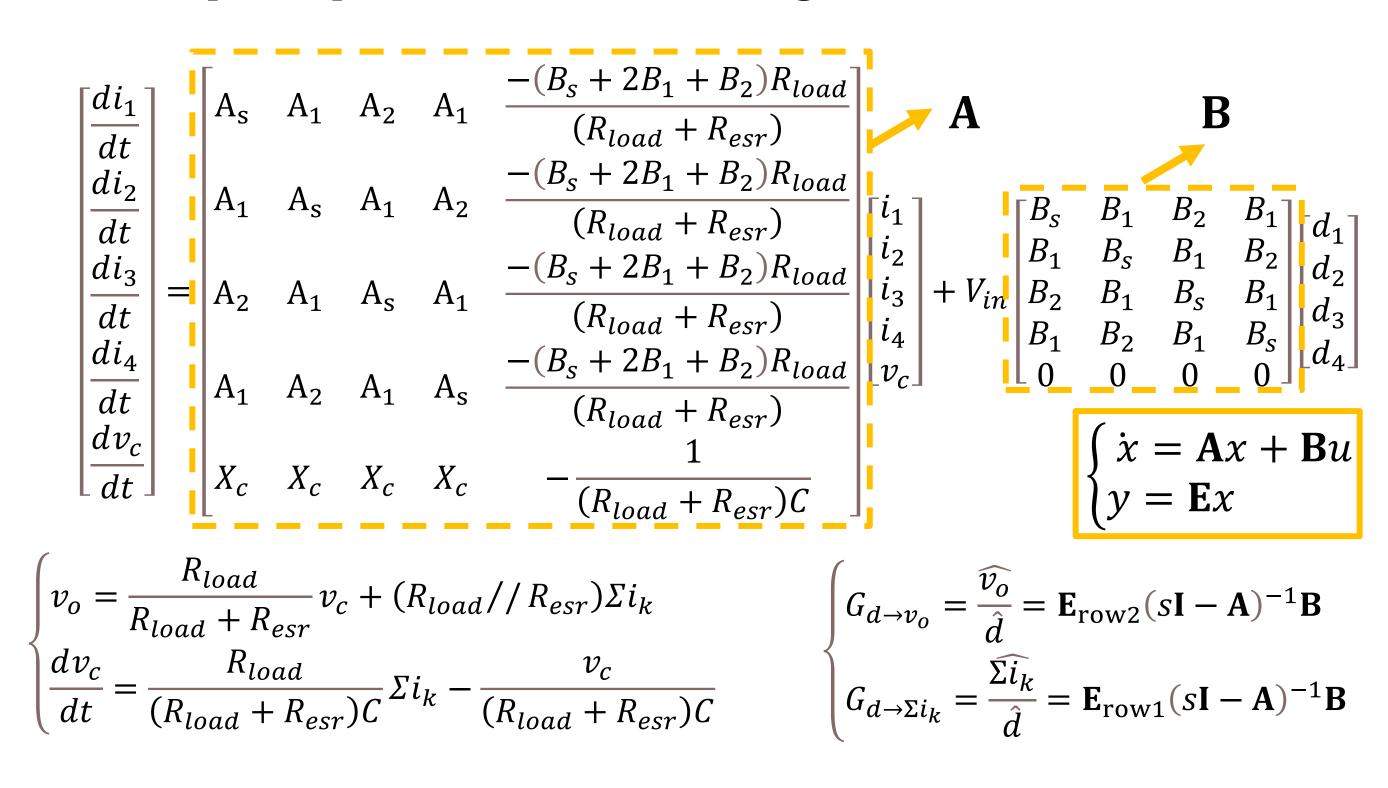
Expression of equivalent interval inductance in all duty cycle ranges

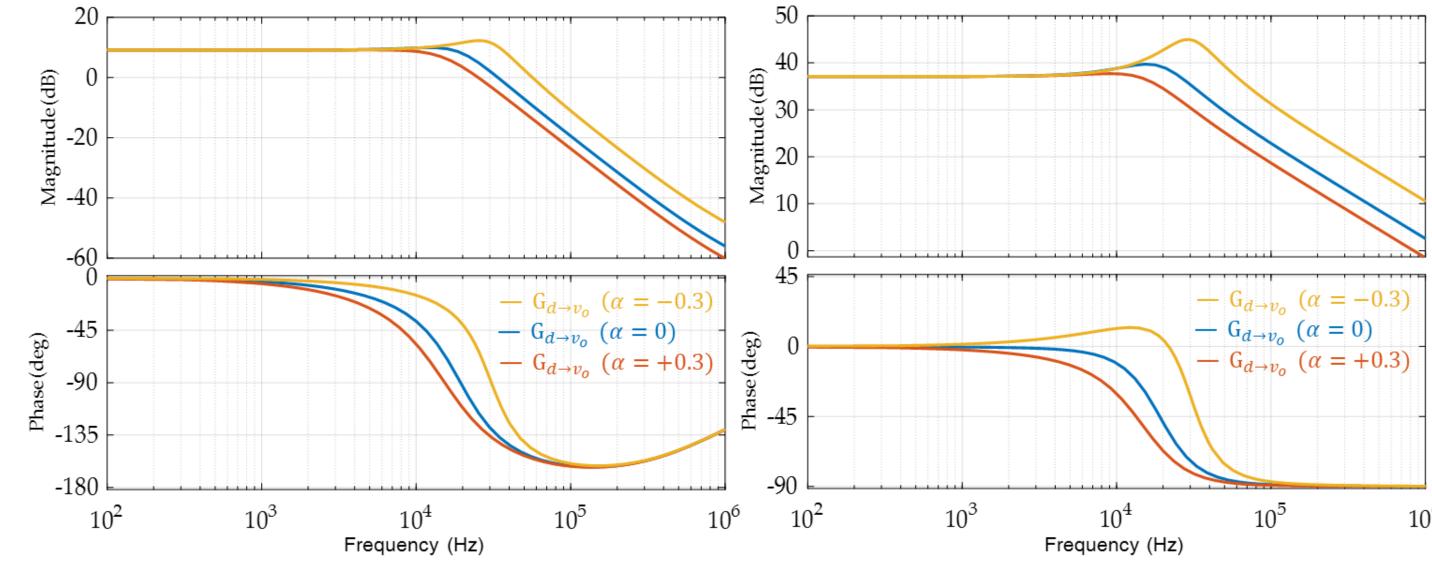
Duty cycle range	Related time interval	Symbol	Expression
0 < D < 0.25	Interval I	$L_{eq1}$	$\frac{(1-D)(4\alpha^2-1)}{2\alpha^2-2D\alpha+(D-1)}L_s$
	Interval II, IV, VI, VIII	$L_{eq2}$	$\frac{\left(4\alpha^2-1\right)}{2\alpha-1}L_s$
	Interval III, VII	$L_{eq3}$	$\frac{(-D)(4\alpha^2-1)}{(1-2D)\alpha+D}L_s$
	Interval V	$L_{eq4}$	$\frac{(-D)(4\alpha^2 - 1)}{-2\alpha^2 - 2D\alpha + D}L_s$
0.75 < D < 1	Interval I	$L_{eq1*}$	$\frac{(-D)(4\alpha^2-1)}{-2\alpha^2+(2-2D)\alpha+D}L_s$
	Interval III, VII	$L_{eq3*}$	$\frac{(1-D)(4\alpha^2-1)}{(1-2D)\alpha+(D-1)}L_s$
	Interval V	$L_{eq4*}$	$\frac{(1-D)(4\alpha^2-1)}{\alpha^2+(2-2D)\alpha+(D-1)}L_s$
0.25 < D < 0.5	Interval I, III	$L_{eq5}$	$\frac{(1-D)(4\alpha^2-1)}{2\alpha^2+(1-2D)\alpha+(D-1)}L_s$
0.5 < D < 0.75	Interval V, VII	$L_{eq6}$	$\frac{D(4\alpha^2-1)}{2\alpha^2+(2D-1)\alpha-D}L_s$

Similar to conventional coupled multiphase buck converter, it is possible to have larger steady-state inductor  $L_{SS}$  and smaller transient inductor  $L_{tr}$ 

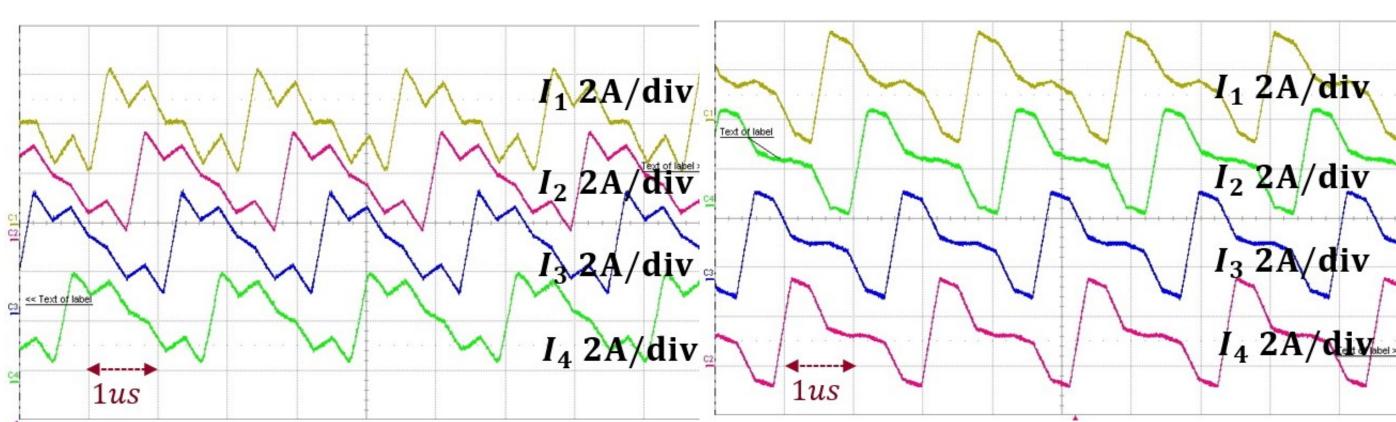


- The proposed coupled inductor dynamic performance in dc-dc converter can be analyzed through state space model, by inverse the inductance matrix  $\mathbf{Z}_{\mathbf{m}}$  to reluctance matrix  $\mathbf{B}$ .
- The duty cycle to output current and output voltage dynamics  $(G_{d \to v_o} \text{ and } G_{d \to \Sigma i_k})$  can be calculated using the derived model. The output capacitor esr and winding resistors are considered.

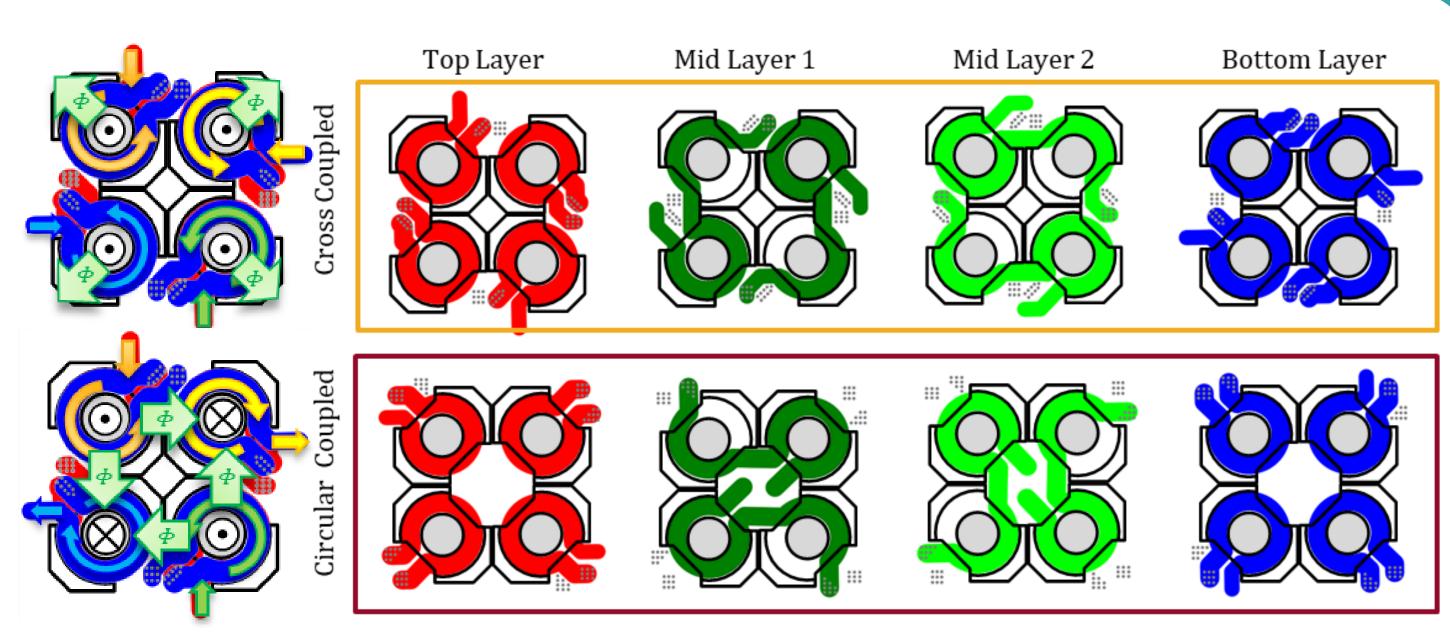




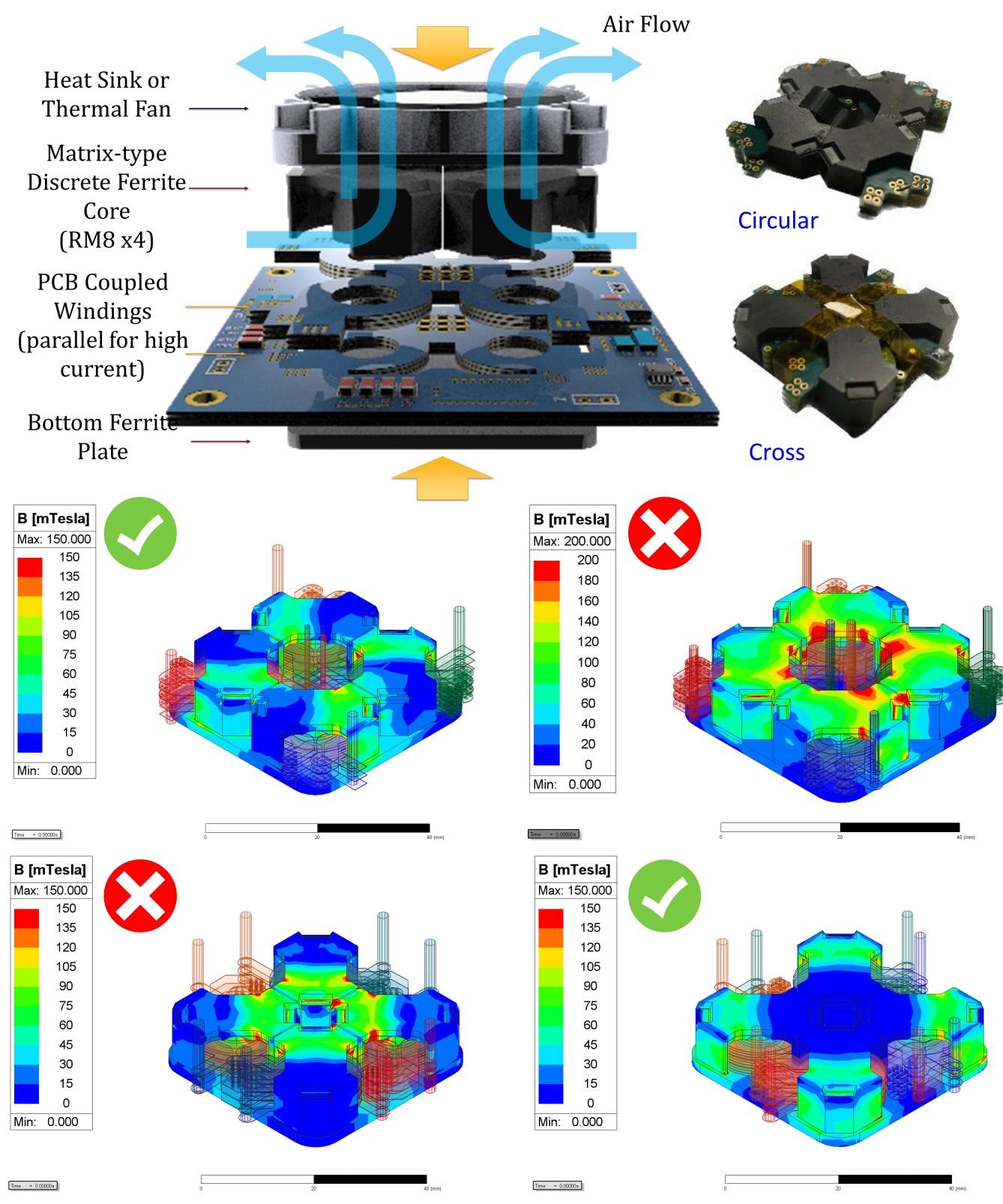
- The 4-phase example shows adjacent negative coupling can broaden the bandwidth, while positive coupling can have the opposite effect.
- Compared with traditional coupling structure, non-adjacent phase coupling has little impact on the system dynamics.



The waveform of discrete symmetrical coupled buck converter shows similar performance to traditional structure, suggesting that it is unnecessary to strictly control geometry symmetry between the phases to obtain a better current sharing and dynamic performance.



The proposed coupling structure can be implemented with matrix-type integration of RM cores, both cross and circular shape coupled.



According FEA simulation, when windings are cross negative coupled, the coupling will be strengthened, otherwise the coupling will be lower. From flux distribution, it is recommended to use cross shape for negative coupled and circular shape for positive coupled.